

Pre-Calculus Summer Review

Evaluate each using the values given.

1) $8k - (k + j^2)$; use $j = 7$, and $k = -3$

2) $-2(y - 8) + \frac{z}{2}$; use $y = 2$, and $z = 2$

Solve each equation by taking square roots.

3) $4r^2 - 3 = 78$

4) $-2 - 10x^2 = -492$

Solve each equation by factoring.

5) $p^2 + 6p + 8 = 0$

6) $n^2 - 6n = 0$

7) $2x^2 - 19x + 24 = 0$

8) $4x^2 + 20 = -21x$

9) $2r^2 - 21 = -11r$

Solve each equation with the quadratic formula.

$$10) \ 5x^2 = -7x + 4$$

$$11) \ 4a^2 + 10a = 66$$

Solve each equation by completing the square.

$$12) \ a^2 - 14a + 45 = 0$$

$$13) \ x^2 - 4x - 59 = 0$$

Factor each completely. (special cases)

$$14) \ 16k^2 - 9$$

$$15) \ 16a^2 - 40a + 25$$

$$16) \ 4a^3 + 256$$

$$17) \ 27x^3 + 1$$

Solve each radical equation. Remember to check for extraneous solutions.

$$18) \ -1 = \sqrt{x-1} - 7$$

$$19) \ \sqrt{b-7} = 5$$

Solve each absolute value equation.

$$20) \ |-7x| = 56$$

$$21) \ |5p| = 40$$

Perform the indicated operation.

$$22) \ -5\sqrt{3}(5 + \sqrt{3})$$

$$23) \ \sqrt{2}(2 + 2\sqrt{2})$$

$$24) \ (-3\sqrt{3} + 2)(\sqrt{3} - 2)$$

$$25) \ (-3\sqrt{3} - 2)(\sqrt{3} - 4)$$

$$26) \ -2 - (3 - 8i) + (4i)$$

$$27) \ (4 - 3i) - (1 - 7i)$$

$$28) \ (-4 - i)(1 + 3i)$$

$$29) \ (5 + 5i)(-1 - 4i)$$

Simplify each expression.

$$30) \frac{5n}{2} - \frac{5n}{6n + 12}$$

$$31) \frac{5}{a+4} - \frac{2a}{a+1}$$

Simplify each rational expression.

$$32) \frac{\frac{m}{9} - \frac{25}{9}}{15}$$

$$33) \frac{\frac{1}{x} - \frac{3}{x-3}}{\frac{9}{x-3}}$$

State the possible number of imaginary zeros and the possible number of positive and negative zeros for each function. Then find all zeros.

$$34) f(x) = x^3 - 2x^2 + x - 12$$

$$35) f(x) = 4x^3 + 8x^2 + 5x + 1$$

Evaluate each expression.

$$36) \log_2 16$$

$$37) \log_2 64$$

Expand each logarithm.

38) $\log_2(a \cdot b \cdot c^4)$

39) $\log_5 \frac{x^4}{y^4}$

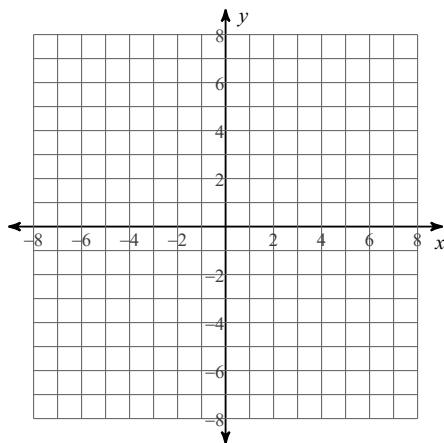
Condense each expression to a single logarithm.

40) $2\log_9 a - 4\log_9 b$

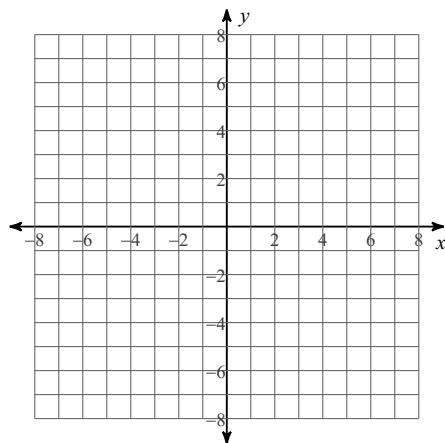
41) $4\log_8 u + 16\log_8 v$

Sketch the graph of each function.

42) $y = \sqrt{x} + 2$

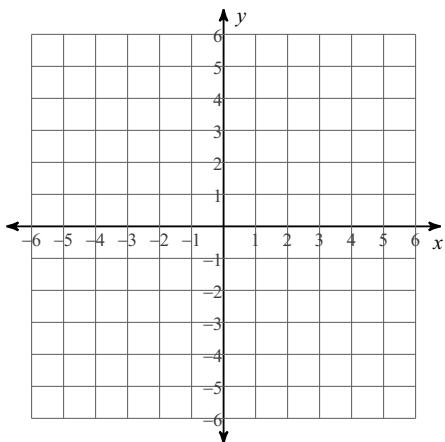


43) $y = \sqrt{x} - 4$

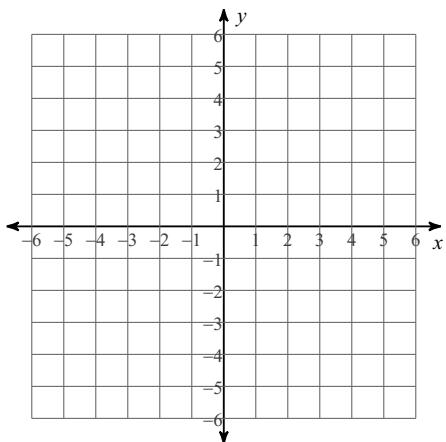


Graph each equation.

44) $y = |x - 3|$

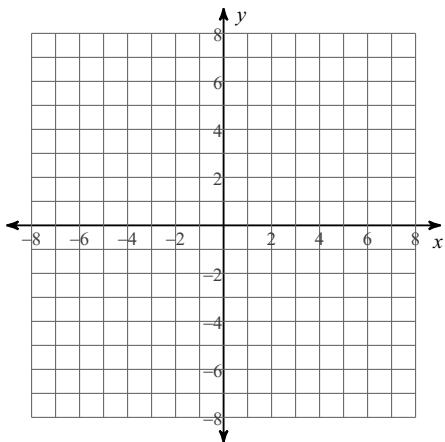


45) $y = |x| - 2$

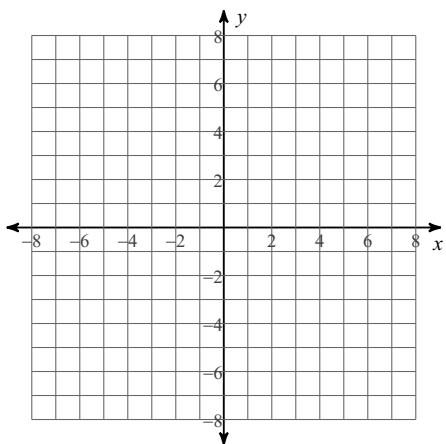


Graphing quadratics (parabolas). Identify the vertex and axis of symmetry of each. Then sketch the graph.

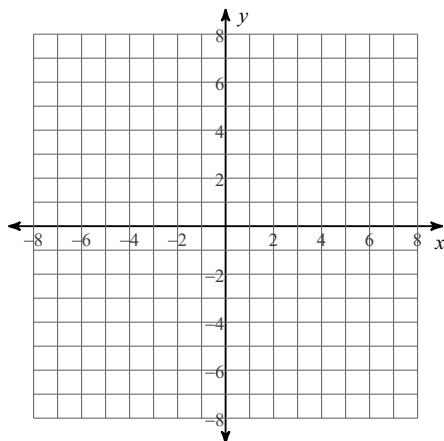
46) $y = x^2 - 12x + 37$



47) $y = -2(x + 1)^2 - 3$

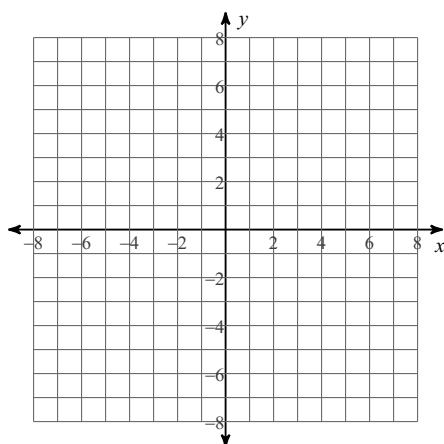


48) $y = -2x^2 - 5$

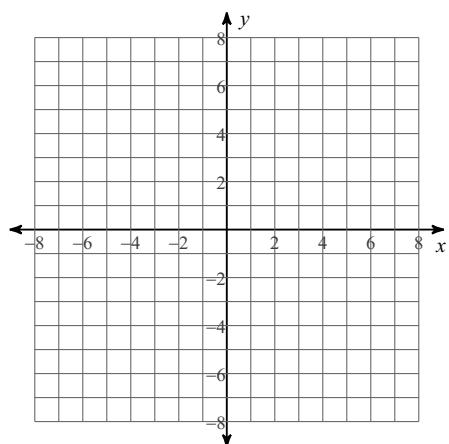


Sketch the graph of each function.

49) $f(x) = x^3 - 4x^2 + 7$



50) $f(x) = -x^3 + x^2 + 1$



Answers to Pre-Calculus Summer Review

1) -70

5) $\{-4, -2\}$

9) $\left\{\frac{3}{2}, -7\right\}$

12) $\{9, 5\}$

15) $(4a - 5)^2$

18) $\{37\}$

22) $-25\sqrt{3} - 15$

26) $-5 + 12i$

30) $\frac{15n^2 + 25n}{6(n+2)}$

34) Possible # of imaginary zeros: 2 or 0

Possible # positive real zeros: 3 or 1

Possible # negative real zeros: 0

Zeros: $\left\{3, \frac{-1+i\sqrt{15}}{2}, \frac{-1-i\sqrt{15}}{2}\right\}$

36) 4

39) $4\log_5 x - 4\log_5 y$

42)

2) 13

6) $\{6, 0\}$

10) $\left\{\frac{-7 + \sqrt{129}}{10}, \frac{-7 - \sqrt{129}}{10}\right\}$

13) $\{2 + 3\sqrt{7}, 2 - 3\sqrt{7}\}$

16) $4(a+4)(a^2 - 4a + 16)$

19) $\{32\}$

23) $2\sqrt{2} + 4$

27) $3 + 4i$

31) $\frac{-2a^2 - 3a + 5}{(a+4)(a+1)}$

20) $\{-8, 8\}$

24) $-13 + 8\sqrt{3}$

28) $-1 - 13i$

32) $\frac{m - 25}{135}$

35) Possible # of imaginary zeros: 2 or 0

Possible # positive real zeros: 0

Possible # negative real zeros: 3 or 1

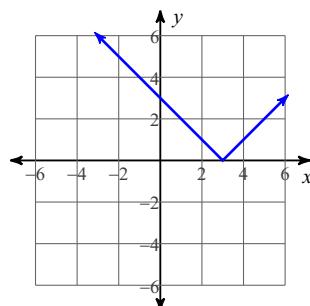
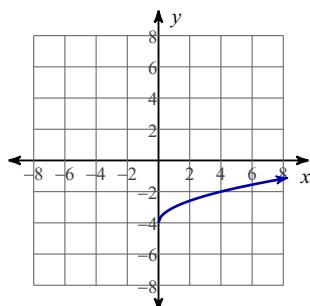
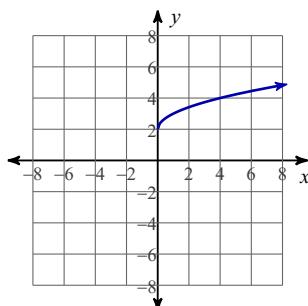
Zeros: $\left\{-\frac{1}{2} \text{ mult. 2}, -1\right\}$

37) 6

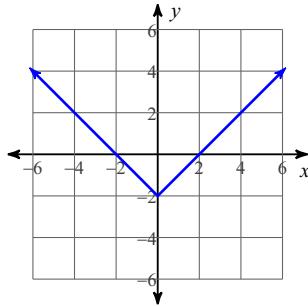
40) $\log_9 \frac{a^2}{b^4}$

43)

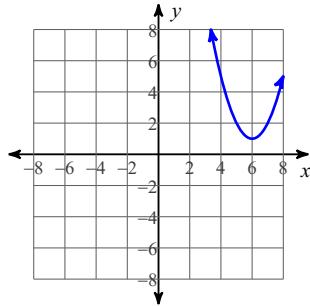
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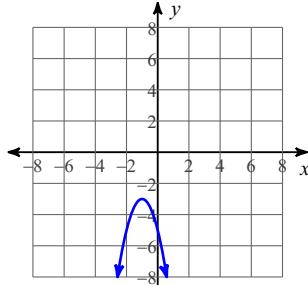
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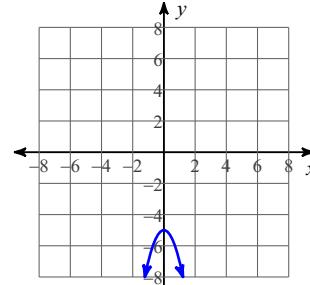
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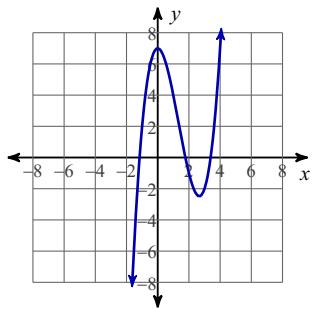
47)



48)



49)



50)

