

## Pre-Calculus Summer Review

**Evaluate each using the values given.**

1)  $8k - (k + j^2)$ ; use  $j = 7$ , and  $k = -3$

2)  $-2(y - 8) + \frac{z}{2}$ ; use  $y = 2$ , and  $z = 2$

**Solve each equation by taking square roots.**

3)  $4r^2 - 3 = 78$

4)  $-2 - 10x^2 = -492$

**Solve each equation by factoring.**

5)  $p^2 + 6p + 8 = 0$

6)  $n^2 - 6n = 0$

7)  $2x^2 - 19x + 24 = 0$

8)  $4x^2 + 20 = -21x$

9)  $2r^2 - 21 = -11r$

**Solve each equation with the quadratic formula.**

$$10) \ 5x^2 = -7x + 4$$

$$11) \ 4a^2 + 10a = 66$$

**Solve each equation by completing the square.**

$$12) \ a^2 - 14a + 45 = 0$$

$$13) \ x^2 - 4x - 59 = 0$$

**Factor each completely. (special cases)**

$$14) \ 16k^2 - 9$$

$$15) \ 16a^2 - 40a + 25$$

$$16) \ 4a^3 + 256$$

$$17) \ 27x^3 + 1$$

**Solve each radical equation. Remember to check for extraneous solutions.**

$$18) \ -1 = \sqrt{x-1} - 7$$

$$19) \ \sqrt{b-7} = 5$$

**Solve each absolute value equation.**

$$20) \ |-7x| = 56$$

$$21) \ |5p| = 40$$

**Perform the indicated operation.**

$$22) \ -5\sqrt{3}(5 + \sqrt{3})$$

$$23) \ \sqrt{2}(2 + 2\sqrt{2})$$

$$24) \ (-3\sqrt{3} + 2)(\sqrt{3} - 2)$$

$$25) \ (-3\sqrt{3} - 2)(\sqrt{3} - 4)$$

$$26) \ -2 - (3 - 8i) + (4i)$$

$$27) \ (4 - 3i) - (1 - 7i)$$

$$28) \ (-4 - i)(1 + 3i)$$

$$29) \ (5 + 5i)(-1 - 4i)$$

**Simplify each expression.**

$$30) \frac{5n}{2} - \frac{5n}{6n + 12}$$

$$31) \frac{5}{a+4} - \frac{2a}{a+1}$$

**Simplify each rational expression.**

$$32) \frac{\frac{m}{9} - \frac{25}{9}}{15}$$

$$33) \frac{\frac{1}{x} - \frac{3}{x-3}}{\frac{9}{x-3}}$$

**State the possible number of imaginary zeros and the possible number of positive and negative zeros for each function. Then find all zeros.**

$$34) f(x) = x^3 - 2x^2 + x - 12$$

$$35) f(x) = 4x^3 + 8x^2 + 5x + 1$$

**Evaluate each expression.**

$$36) \log_2 16$$

$$37) \log_2 64$$

**Expand each logarithm.**

38)  $\log_2(a \cdot b \cdot c^4)$

39)  $\log_5 \frac{x^4}{y^4}$

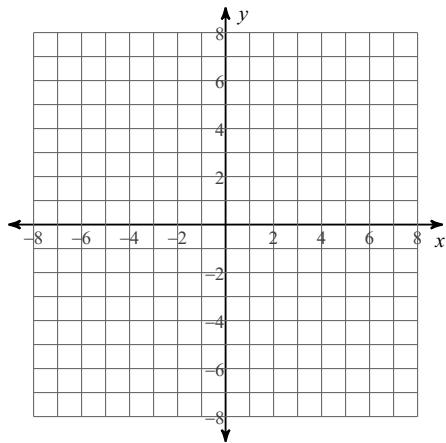
**Condense each expression to a single logarithm.**

40)  $2\log_9 a - 4\log_9 b$

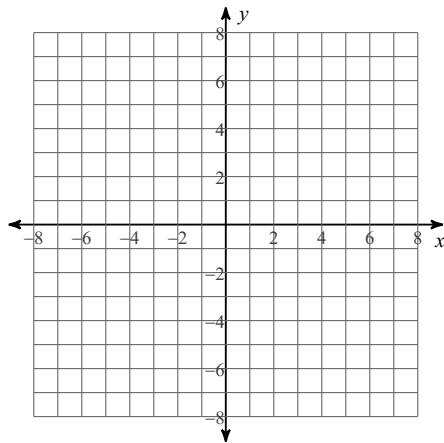
41)  $4\log_8 u + 16\log_8 v$

**Sketch the graph of each function.**

42)  $y = \sqrt{x} + 2$

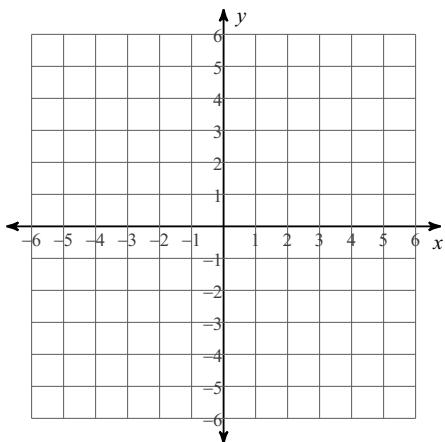


43)  $y = \sqrt{x} - 4$

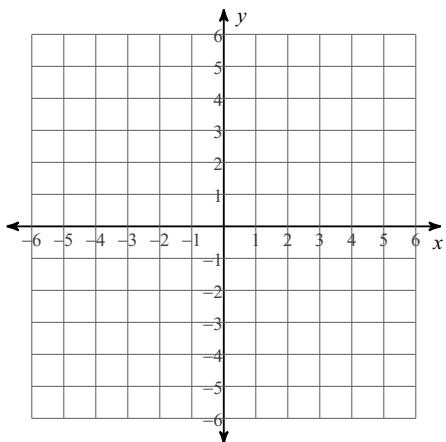


**Graph each equation.**

44)  $y = |x - 3|$

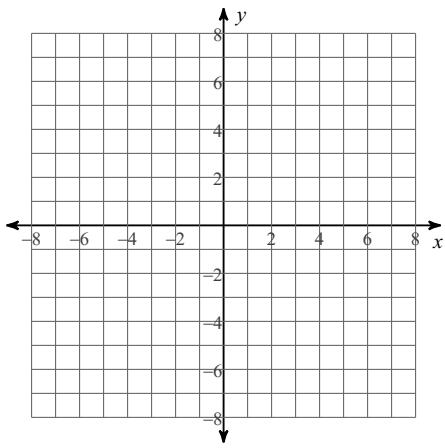


45)  $y = |x| - 2$

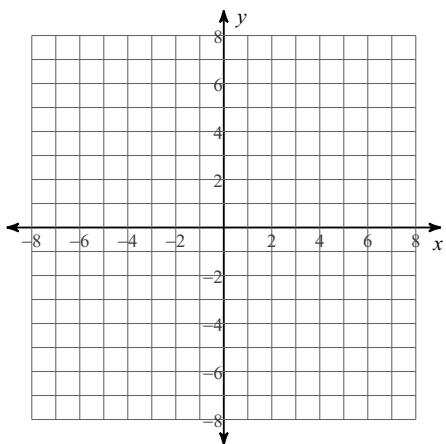


**Graphing quadratics (parabolas). Identify the vertex and axis of symmetry of each. Then sketch the graph.**

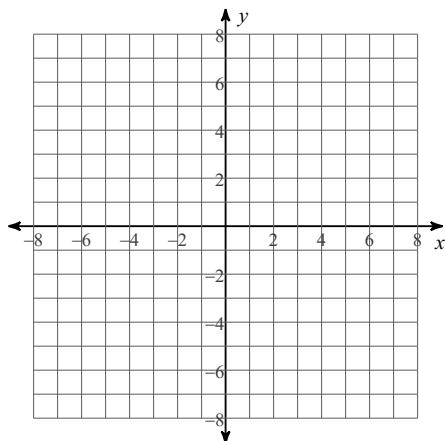
46)  $y = x^2 - 12x + 37$



47)  $y = -2(x + 1)^2 - 3$

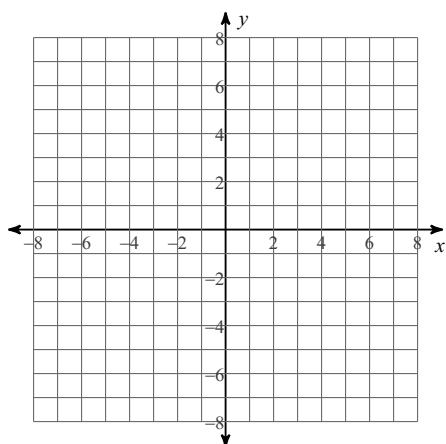


48)  $y = -2x^2 - 5$

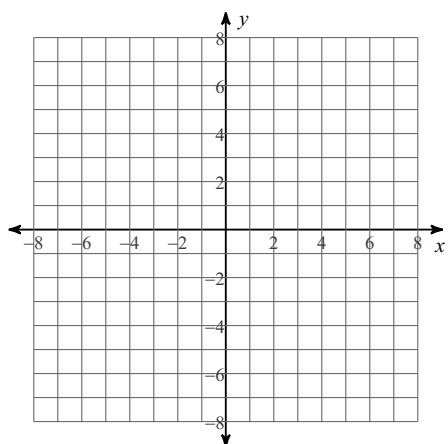


**Sketch the graph of each function.**

49)  $f(x) = x^3 - 4x^2 + 7$



50)  $f(x) = -x^3 + x^2 + 1$



# Answers to Pre-Calculus Summer Review

1)  $-70$

5)  $\{-4, -2\}$

9)  $\left\{\frac{3}{2}, -7\right\}$

12)  $\{9, 5\}$

15)  $(4a - 5)^2$

18)  $\{37\}$

22)  $-25\sqrt{3} - 15$

26)  $-5 + 12i$

30)  $\frac{15n^2 + 25n}{6(n+2)}$

34) Possible # of imaginary zeros: 2 or 0

Possible # positive real zeros: 3 or 1

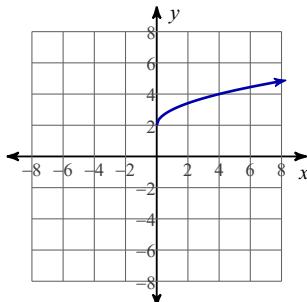
Possible # negative real zeros: 0

Zeros:  $\left\{3, \frac{-1+i\sqrt{15}}{2}, \frac{-1-i\sqrt{15}}{2}\right\}$

36) 4

39)  $4\log_5 x - 4\log_5 y$

42)



2) 13

6)  $\{6, 0\}$

10)  $\left\{\frac{-7+\sqrt{129}}{10}, \frac{-7-\sqrt{129}}{10}\right\}$

13)  $\{2+3\sqrt{7}, 2-3\sqrt{7}\}$

16)  $4(a+4)(a^2-4a+16)$

19)  $\{32\}$

23)  $2\sqrt{2} + 4$

27)  $3+4i$

31)  $\frac{-2a^2 - 3a + 5}{(a+4)(a+1)}$

20)  $\{-8, 8\}$ 

24)  $-13 + 8\sqrt{3}$

28)  $-1 - 13i$

32)  $\frac{m-25}{135}$

35) Possible # of imaginary zeros: 2 or 0

Possible # positive real zeros: 0

Possible # negative real zeros: 3 or 1

Zeros:  $\left\{-\frac{1}{2} \text{ mult. 2}, -1\right\}$

37) 6

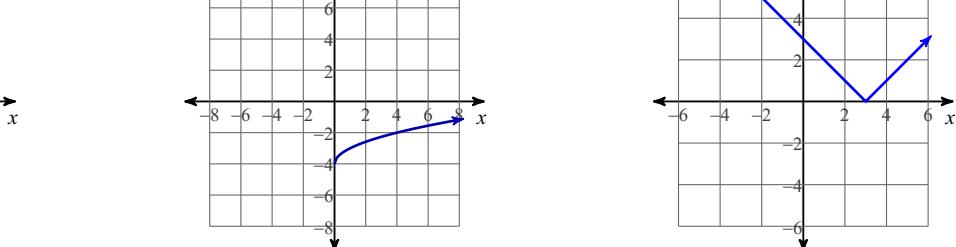
40)  $\log_9 \frac{a^2}{b^4}$

43)

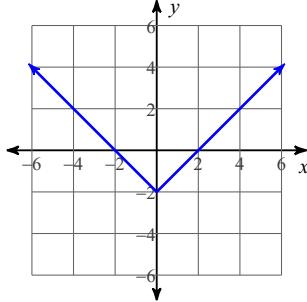
38)  $\log_2 a + \log_2 b + 4\log_2 c$

41)  $\log_8(v^{16}u^4)$

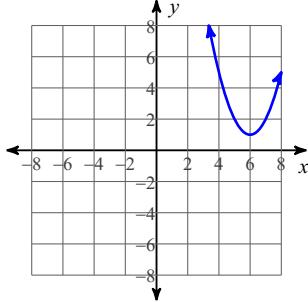
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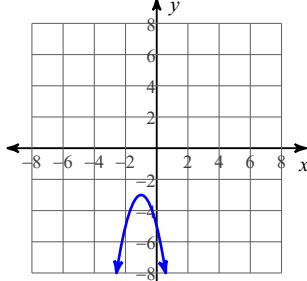
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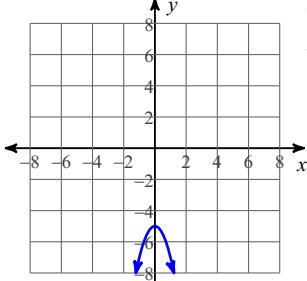
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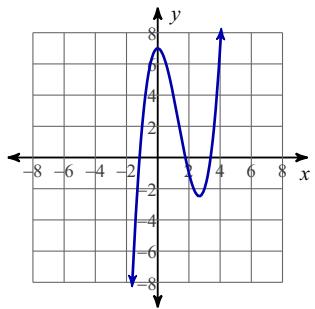
47)



48)



49)



50)

